



## Summary

- We present the induced generative adversarial particle transformer (iGAPT) for **jet simulation**.
- Physics-informed inductive biases, conditioning on global jet features, and induced attention mechanism achieves high-fidelity, demonstrating **competitive performance** with SOTA models on simulating 30-particle jets.
- Significantly better **computational efficiency** and **time complexity**.
- Exhibits strong potential to simulate **larger numbers of particles**, being able to simulate 150-particle jets, which is not achievable using previous model (MPGAN).

## Machine Learning for CERN LHC Simulations

- In **high energy physics** (HEP), jets generated by particle collisions at the Large Hadron Collider (LHC) helps the understanding of particle properties and identification of rare particles.
- ML models have advantages in simulating these collisions. The message-passing GAN (MPGAN) made significant strides by using graph neural networks to handle variable-sized particle clouds, but has **quadratic time complexity**.
- Generative Adversarial Particle Transformer (GAPT) improved the efficiency using self-attention blocks, but could not match MPGAN's performance.

## Dataset: JetNet

- Includes simulated high transverse-momentum ( $p_T$ ) jets from various sources like gluons, light quarks, and top quarks.
- Each jet is represented as a point cloud of its constituent particles, characterized by three features: relative angular coordinates ( $\eta^{rel}$ ,  $\phi^{rel}$ ), and transverse-momentum ( $p_T$ ).
  - Gluon: Baseline generation test
  - Light quarks: Fewer particles; variable-sized clouds test
  - Top quark: Complex topology

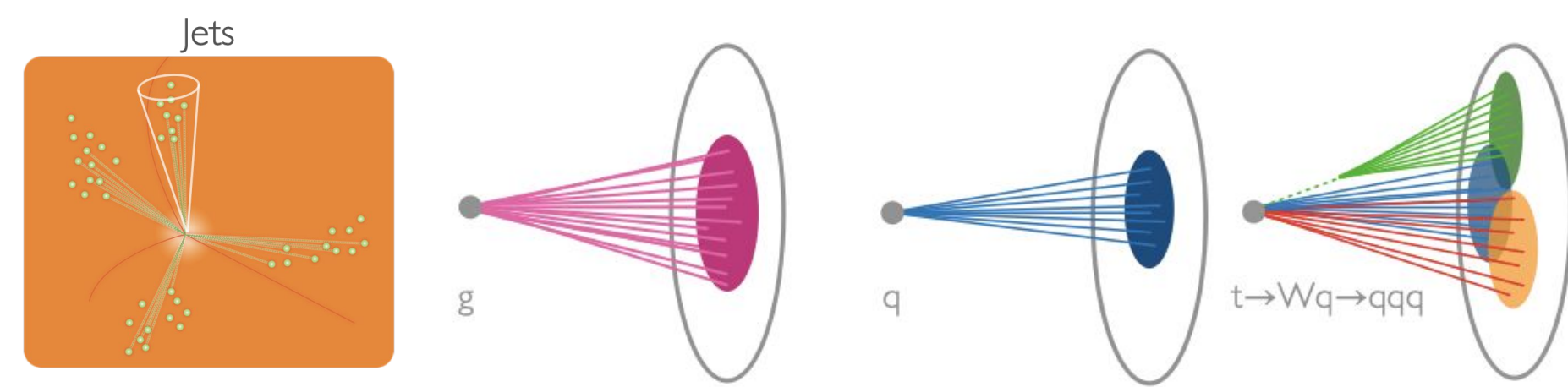


Figure 1: Jets (left) and JetNet (right)

## Induced Generative Adversarial Particle Transformers (iGAPT)

The key ideas in iGAPT:

- Particle cloud representations effectively represent **sparsity** and **permutation symmetry** of jets
- Induced set attention blocks** offers **linear scaling** with number of particles.
- Learning **global jet features** through induced particle attention blocks (IPABs)

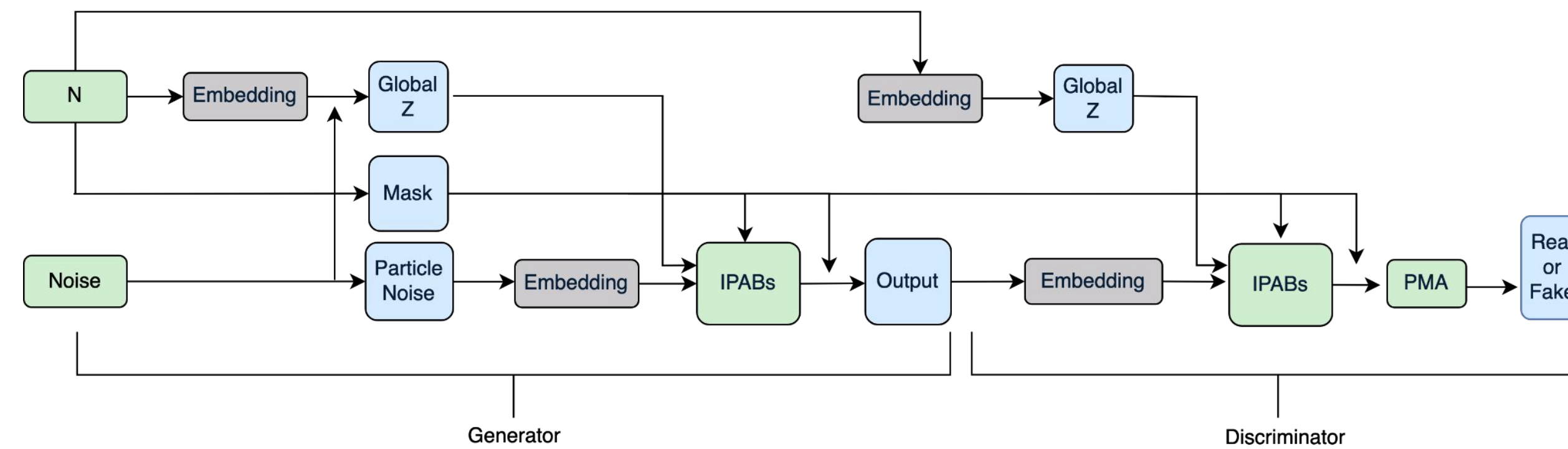


Figure 2: Structure of iGAPT Model

- Global z**: A global conditioning vector learnt and maintained through the generation and discrimination to implicitly **represent global jet features**.
- PMA**: Pooling by Multihead Attention layer that aggregates the intermediate representation in a **permutation-invariant** way.
- IPABs**: Induced Particle Attention Blocks. The global vector  $z$  is used as the **inducing vector** to attend the input, outputting an compressed representation.  $z$  is **continuously updated** through the attention outputs, allowing the update and learning of global jet features and individual particle features interactively in each attention layer.

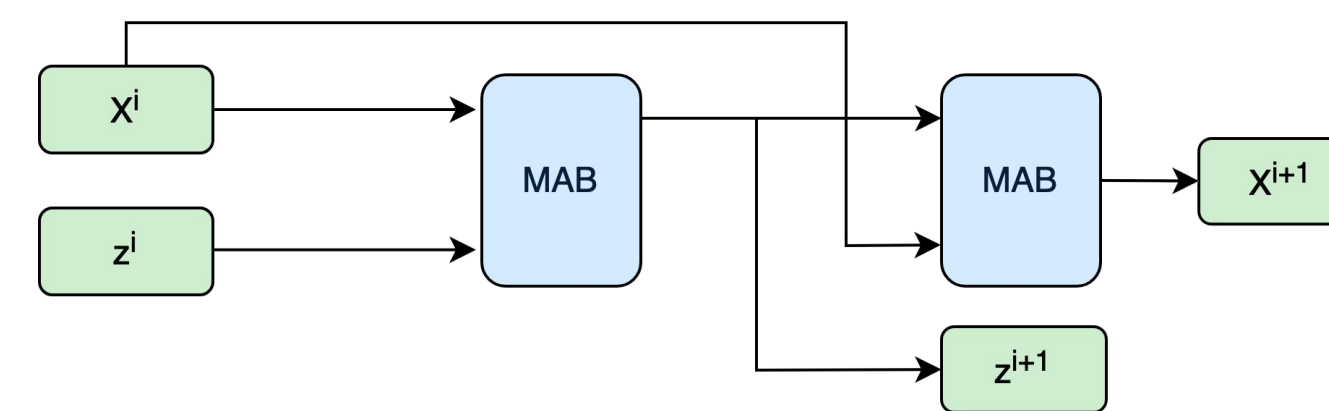


Figure 3: Structure of IPAB

## Evaluation

- We evaluate the performance by **Fréchet physics distance** (FPD), **kernel physics distance** (KPD), and **1-Wasserstein distances** ( $W_1$ ) between individual particle and jet features
- Sensitive metrics to comprehensively evaluate generative HEP model performance.
- Also includes visual comparison of **feature distributions** between the real and generated samples.

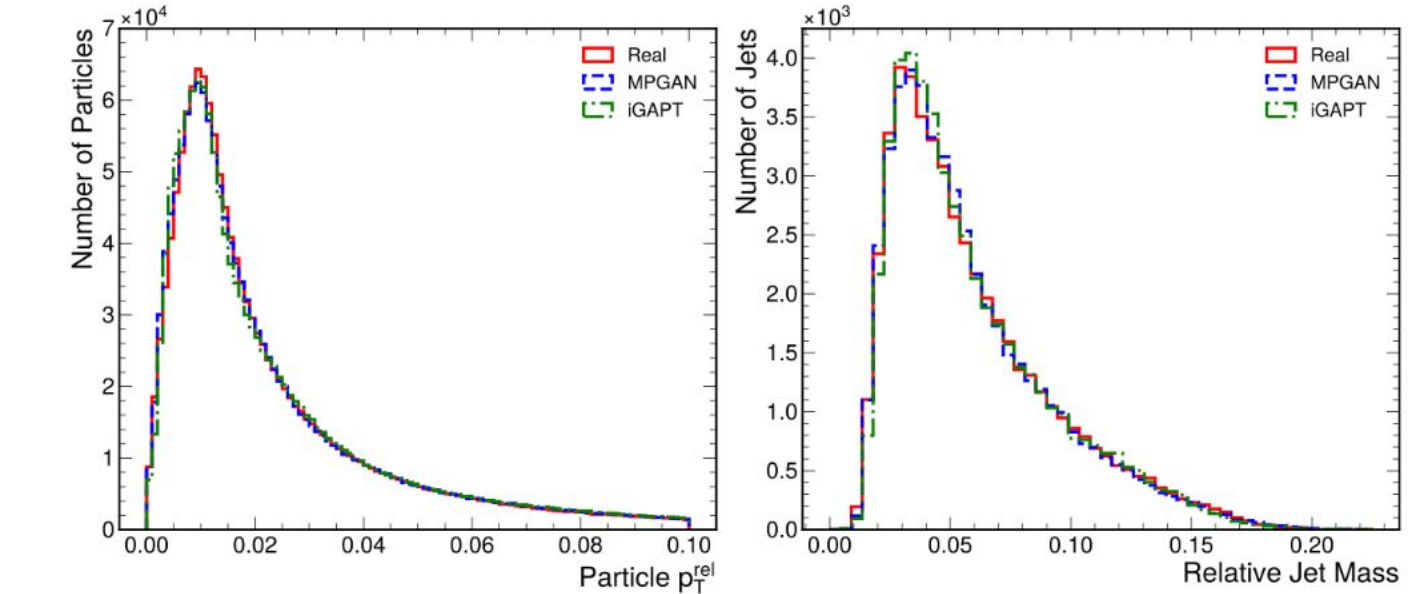
## Timing Measurements

- The table below shows the training time and inference time for **30-particle gluon** measured on an NVIDIA 1080 GPU.

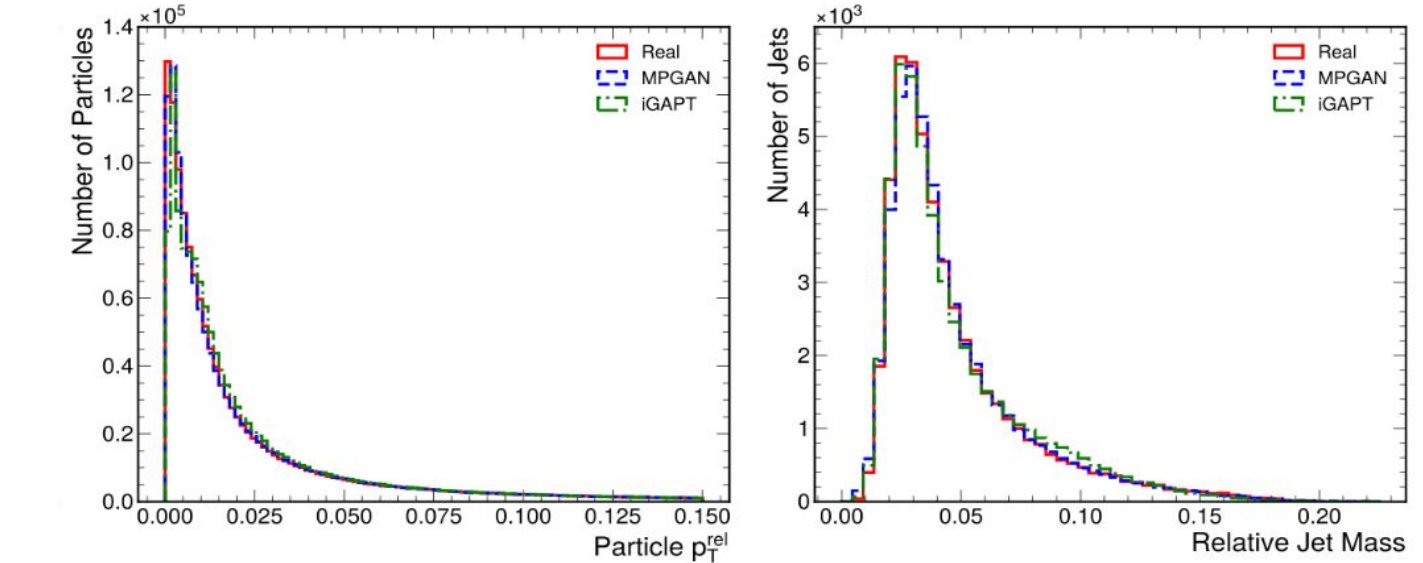
Model	Training time	Generation time	Batch size
MPGAN	193 (s/epoch)	142 ( $\mu$ s / jet)	512
iGAPT	<b>31 (s/epoch)</b>	<b>40 (<math>\mu</math>s / jet)</b>	4096

## Results

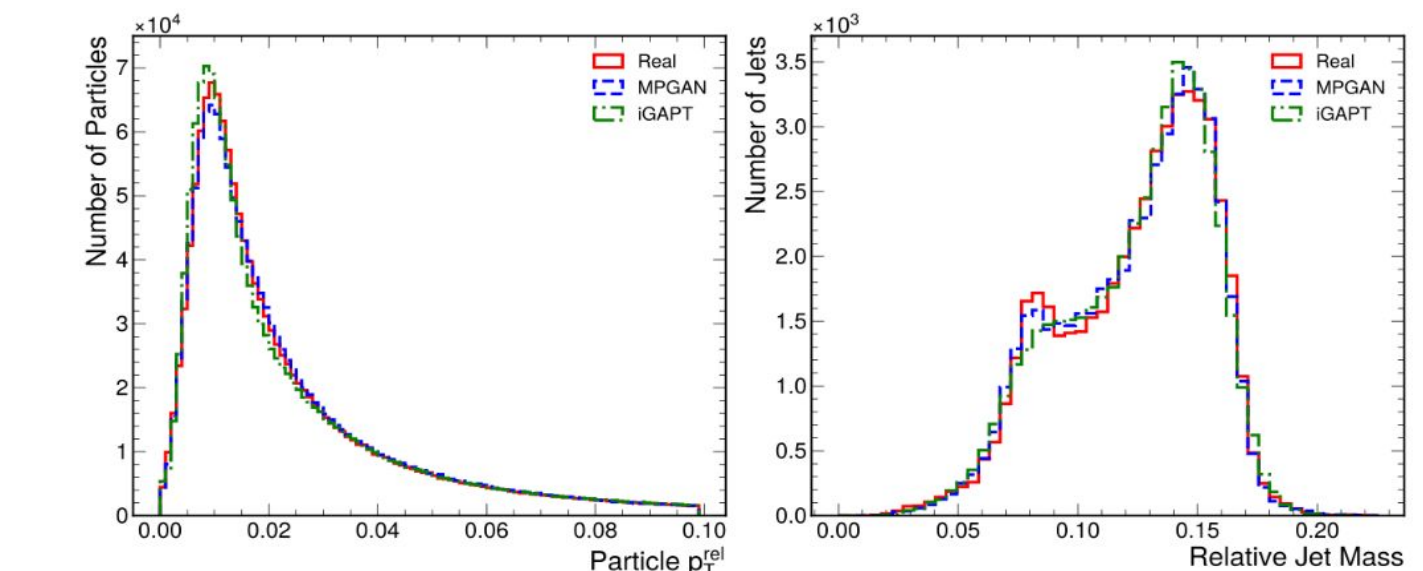
- Particle feature distributions for **30-particle gluon**:



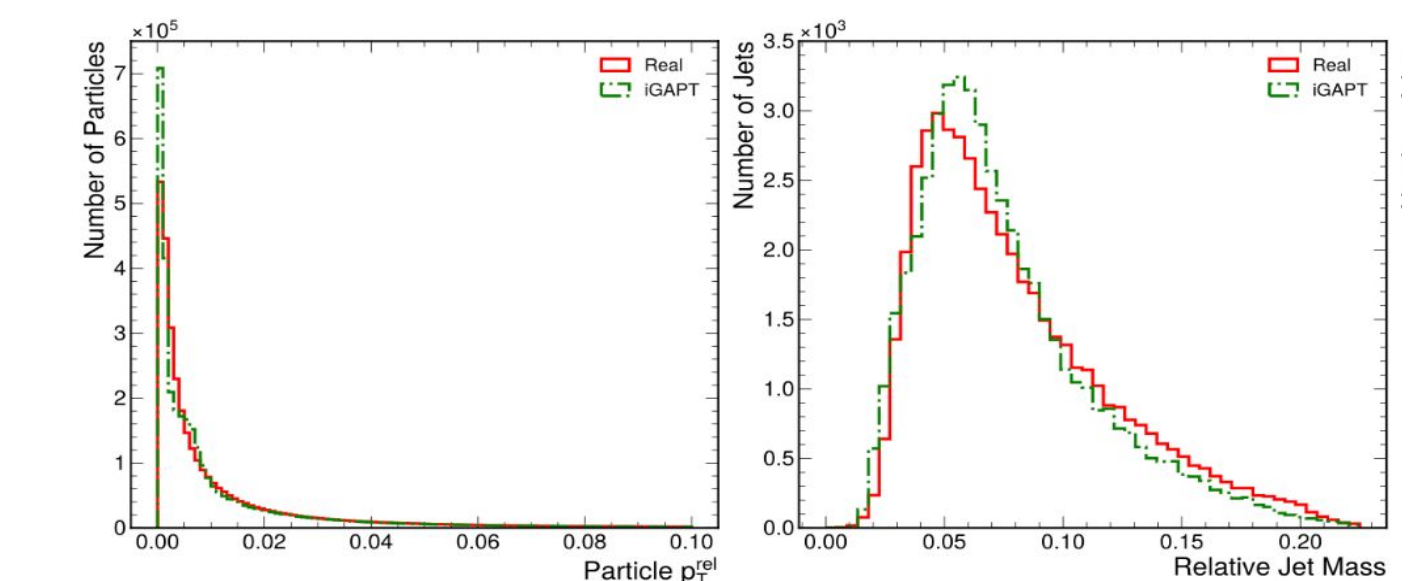
- Particle feature distributions for **30-particle light quark**:



- Particle feature distributions for **30-particle top quark jets**:



- Particle feature distributions for **150-particle gluon** (MPGAN was unable to simulate due to high computational complexity):



- Evaluation metrics for different and models on **30-particle gluon**

Model	$W_1^p(10^{-3})$	$W_1^M(10^{-3})$	FPD ( $10^{-3}$ )	KPD ( $10^{-6}$ )
Truth	$0.14 \pm 0.06$	$0.46 \pm 0.08$	$0.14 \pm 0.04$	$1.8 \pm 11.9$
MPGAN	$0.27 \pm 0.02$	$0.7 \pm 0.3$	$0.41 \pm 0.09$	<b><math>0 \pm 8</math></b>
GAPT	<b><math>0.25 \pm 0.07</math></b>	$1.0 \pm 0.2$	$0.46 \pm 0.06$	$5 \pm 3$
iGAPT	$0.76 \pm 0.07$	<b><math>0.7 \pm 0.1</math></b>	<b><math>0.29 \pm 0.04</math></b>	$3 \pm 5$